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UTILITY
PATENT APPLICATION
TRANSMITTAL

(Only for new nonprovisional applications under 37 CFR 1.53(b))

Attorney Docket No.	TI-31367
First Named Inventor or Application Identifier	Arthur J. Redfern
Title	Multi-Channel Frequency Domain Equalizer For Radio Frequency Interference Cancellation
Express Mail Label No.	EL547741644US

APPLICATION ELEMENTS

See MPEP Chapter 600 concerning utility patent application contents

ADDRESS TO:
Assistant Commissioner for Patents
Box Patent Application
Washington, DC 20231

1. [X] *Fee Transmittal Form (e.g., PTO/SB/17)
(Submit an original, and a duplicate for fee processing)

2. [X] Specification   [Total Pages 18]
(preferred arrangement set forth below)
- Descriptive title of the Invention
- Cross References to Related Applications
- Statement Regarding Fed sponsored R&D
- Reference to Microfiche Appendix
- Background of the Invention
- Brief Summary of the Invention
- Brief Description of the Drawings (if filed)
- Detailed Description
- Claim(s)
- Abstract of the Disclosure

3. [X] Drawing(s) (35 USC d113)·   [Total Sheets 3]

4. Oath or Declaration   [Total Pages 1]

a. [X] Newly Executed (original or copy)

b. [ ] Copy from a prior application (37 CFR §1.63(d))
(for continuation/divisional with Box 17 completed)

[Note Box 5 below]

i. [ ] DELETION OF INVENTOR(S)
Signed statement attached deleting inventor(s)
named in the prior application,
see 37 CFR §1.63(d)(2) and 1.33(b)

5. [ ] Incorporation By Reference (useable if Box 4b is checked)
The entire disclosure of the prior application, from which a copy of
the oath or declaration is supplied under Box 4b, is considered as
being part of the disclosure of the accompanying application and is
hereby incorporated by reference therein.

6. [ ] Microfiche Computer Program (Appendix)

7. Nucleotide and/or Amino Acid Sequence Submission
(if applicable, all necessary)

a. [ ] Computer Readable Copy

b. [ ] Paper Copy (identical to computer copy)

c. [ ] Statement verifying identical of above copies

ACCOMPANYING APPLICATION PARTS

8. [X] Assignment Papers (cover sheet & Documents(s))

9. [ ] 37 CFR §3.73(b) Statement (when there is an assignee) [X] Power of Attorney

10. [ ] English Translation Document (if applicable)

11. [ ] Information Disclosure Statement (IDS)/PTO-1449   [ ] Copies of IDS Citations

12. [ ] Preliminary Amendment

13. [X] Return Receipt Postcard (MPEP 503)
(Should be specifically itemized)

14. [ ] *Small Entity Statement(s) (PTO/SB/09-12)   [ ] Statement filed in prior application Status still proper and desired

15. [ ] Certified Copy of Priority Document(s) if foreign priority is claimed)

16. [ ] Other:

*A new statement is required to be entitled to pay small entity fees, except
where one has been filed in a prior application and is being relied upon

17. If a CONTINUING APPLICATION, check appropriate box and supply the requisite information below and in a preliminary amendment:

[ ] Continuation   [ ] Divisional   [ ] Continuation-in-part (CIP)   of prior application No: ___/___.

Prior application information: Examiner _____   Group / Art Unit: _____

18. CORRESPONDENCE ADDRESS

23494

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ZIP CODE

Name (Print/Type)	Dwight N. Holmbo	Registration No. (Attorney/Agent)	36,410
Signature	Dwight N. Holmbo	Date	11-7-00

PTO/SB/17 (1/98)
Approved for use through 09/30/2000. OMB 0651-0032
Patent and Trademark Office: U.S. DEPARTMENT OF COMMERCE
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FEE TRANSMITTAL

Patent fees are subject to annual revision on October 1.
These are the fees effective October 1, 1997
Small Entity payments must be supported by a small entity statement,
otherwise large entity fees must be paid. See Forms PTO/SB/09-12.

Complete If Known	
Application Number	N/A
Filing Date	11/07/00
First Named Inventor	Arthur J. Redfern
Examiner Name	N/A
Group / Art Unit	N/A
Attorney Docket No.	TI-31367

TOTAL AMOUNT OF PAYMENT ($) 710.00

METHOD OF PAYMENT

1. ☒ The Commissioner is hereby authorized to charge to the following Deposit Account,

Deposit Account Number: **20-0668**

Deposit Account Name: **Texas Instruments Incorporated**

☒ Charge any additional fee required or credit any overpayment

☐ Charge all indicated fees and any additional fee required or credit any overpayment

2. ☐ **Payment Enclosed:**

☐ Check   ☐ Money Order   ☐ Other

FEE CALCULATION

1. BASIC FILING FEE

Large Fee Code	Entity Fee ($)	Small Fee Code	Entity Fee ($)	Fee Description	Fee Paid
101	710	201	355	Utility filing fee	$710
106	320	206	160	Design filing fee	$
107	490	207	245	Plant filing fee	$
108	710	208	355	Reissue filing fee	$
114	150	214	75	Provisional filing fee	$

SUBTOTAL (1) ($)710.00

2. EXTRA CLAIM FEES

	Extra Claims		Fee from below		Fee Paid
Total Claims	16	-20**=	0	x 18 =	0
Independent Claims	2	-3** =	0	x 80 =	0
Multiple Dependent				270 =	0

**or number previously paid, if greater; For Reissue, see below*

Large Fee Code	Entity Fee ($)	Small Fee Code	Entity Fee ($)	Fee Description
103	18	203	9	Claims in excess of 20
102	80	202	40	Independent Claims in excess of 3
104	270	204	135	Multiple dependent claims in excess of 3
109	80	209	40	**Reissue independent claims over original patent
110	18	210	9	**Reissue claims in excess of 20 and over original patent

SUBTOTAL (2) ($)0

FEE CALCULATION (continued)

3. ADDITIONAL FEES

Large Fee Code	Entity Fee ($)	Small Fee Code	Entity Fee ($)	Fee Description	Fee Paid
105	130	205	65	Surcharge - late filing fee	
127	50	227	25	Surcharge - late provisional filing fee or cover sheet.	
139	130	139	130	Non-English specification	
147	2,520	147	2,520	For filing a request for reexamination	
112	920*	112	920*	Requesting publication of SIR prior to Examiner action	
113	1,840*	113	1,840*	Requesting publication of SIR after Examiner action	
115	110	215	55	Extension for reply within first month	
116	400	216	200	Extension of time within second month	
117	950	217	475	Extension of time within third month	
118	1,510	218	755	Extension of time within fourth month	
128	2,060	228	1,030	Extension of time within fifth month	
119	310	219	155	Notice of Appeal	
120	310	220	155	Filing a brief in support of an appeal	
121	270	221	135	Request for oral hearing	
138	1,510	138	1,510	Petition to institute a pubic use proceeding	
140	110	240	55	Petition to revive - unavoidable	
141	1,320	241	660	Petition to revive - unintentional	
142	1,320	242	660	Utility issue fee (or reissue)	
143	450	243	225	Design issue fee	
144	670	244	335	Plant issue fee	
122	130	122	130	Petitions to the Commissioner	
123	50	123	50	Petitions related to provisional applications	
126	240	126	240	Submission of Information Disclosure Stmt.	
581	40	581	40	Recording each patent assignment per properly (time number of properties)	
146	790	246	395	Filing a submission after final rejection (37 CFR 1 129(a))	
149	790	249	395	For each additional invention to be examined (37 CFR 1.129(b))	

Other fee (specify) _____

Other fee (specify) _____

*Reduced by Basic Filing Fee Paid

SUBTOTAL (3) _____

SUBMITTED BY			Complete (if applicable)	
Typed or Printed Name	Dwight N. Holmbo		Reg. Number	36,410
Signature	*Dwight N. Holmbo*	Date 11-7-00	Deposit Account User ID	N/A

MULTI-CHANNEL FREQUENCY DOMAIN EQUALIZER
FOR RADIO FREQUENCY INTERFERENCE CANCELLATION

Background of the Invention

1. Field of the Invention

This invention relates generally to radio frequency interference impairments associated with digital subscriber lines, and more particularly to a method for exploiting deterministic spreading of the fast Fourier transform (FFT) at the receiver to cancel correlated noise sources such as RFI.

2. Description of the Prior Art

ITU Telecommunications Standardization Sector, *G.test.bis.*, Study Group 4, Question 15, 1999, has proposed various radio frequency interference (RFI) impairments for incorporation into digital subscriber line (DSL) performance tests. For asymmetric DSL (ADSL) systems such as described in ITU Telecommunications Standardization Sector, *G.992.1: Asymmetrical Digital Subscriber Line (ADSL) Transceivers.*, Study Group 4, Question 15, 2000, RFI is assumed to be caused by narrowband amplitude modulated (AM) radio stations, which overlap the downstream ADSL band from 540-1104 kHz. Additional RFI sources include, but are not limited to, aliases from AM stations operating above 1104 kHz, amateur (HAM) transmitters, televisions, computer equipment, and various other (relatively) low frequency signals (e.g., aeronautical radiolocation signals).

At the ADSL transmitter, data is assembled into subchannels, transformed by an inverse fast Fourier transform (IFFT), and a cyclic prefix is added. After propagating through a communication channel, the opposite operations are performed by the receiver. The cyclic prefix is removed, and the received data is transformed by the fast Fourier transform (FFT). If the communication channel is shorter than the cyclic prefix and the noise is uncorrelated on the individual subchannels, then the transmitted data can be recovered by a one-tap equalizer (the frequency-domain equalizer or FEQ), such as

described by T. Starr, J. Cioffi and P. Silverman, *Understanding Digital Subscriber Line Technology*, Upper Saddle River, NJ: Prentice Hall, 1999.

The noise that results from RFI at the receiver is deterministically spread by the FFT to neighboring subchannels. As a result, instead of one (or a few) subchannels being effected by the narrowband impairment, many subchannels are effected. The resulting loss of signal-to-noise ratio (SNR) can unacceptably limit the capacity of the communication channel.

In view of the foregoing, a need exists for a scheme to exploit the deterministic spreading of the FFT at the receiver to cancel correlated noise sources such as RFI in order to increase the effective data communication rate between subscribers using shared media.

Summary of the Invention

The present invention is directed to a method of estimating the multichannel FEQ in block and iterative fashions. Specifically, algorithms are developed to estimate the multichannel FEQ. The estimated multichannel FEQ provides improvements in SNR over that achievable using standard single channel FEQ.

According to one embodiment, a multichannel FEQ is formulated when there is correlation in the noise matrix (e.g., from a correlated noise source such as RFI). Equalizers which have nonzero elements in addition to the main diagonal are considered. Each row of the multichannel FEQ is recovered via choosing the nonzero columns in addition to the column directly correlated with the input through the channel. Columns corresponding to subchannels having strong correlations with the column directly correlated with the input through the channel are most preferably chosen (generally neighboring subchannels, or subchannels corresponding to strong RFI sources). As the RFI and signal power become closer, not transmitting data on a subchannel allows that subchannel to be used more effectively with other subchannels in the multichannel FEQ.

As used herein, FEQ means a complex multiply to adjust for the gain and phase of the effective channel response in each sub-symbol. The FEQ does not enhance the SNR; it only scales and rotates each sub-symbol so that a common decoder can be used.

As used herein the following notation will have the following meanings. Italics will be used for scalars, and boldface for vectors and matrices. A superscript $^{-1}$ will refer to the pseudoinverse, $*$ to conjugation, ^{T} to transpose, and ^{H} to conjugate transpose. The operator diag() forms a diagonal matrix with the arguments being the elements of the main diagonal, wherein E[] is the expected value of its argument, and $\lambda_{max}()$ is the maximum eigenvalue of its argument. The term $a{:}b$ will be used to denote a contiguous subset of a vector or dimension of a matrix, and a ":" by itself refers to all of the elements along that dimension. For example, if

$$\mathbf{c} = [c(1) \ ... \ c(\mathrm{L})]^{T},$$

then,

$\mathbf{c}(:) = \mathbf{c}$, and

$$\mathbf{c}(a\!:\!b) = [c(a) \ldots c(b)]^{T}.$$

To select a (possibly) noncontiguous subset of a vector or dimension of a matrix, a vector of the desired indices will be used as the argument of that dimension. For example, if

$$\mathbf{k} = [k(1) \ldots k(M)]^{T}$$

is a vector of integers, then

$$\mathbf{c(k)} = [c(k(1)) \ldots c(k(M))]^{T}.$$

Brief Description of the Drawings

Other aspects and features of the present invention, and many of the attendant advantages of the present invention, will be readily appreciated as the same become better understood by reference to the following detailed description when considered in connection with the accompanying drawing wherein:

Figure 1 is a graph illustrating a simulated subchannel SNR for additive white Gaussian noise (AWGN) with no RFI, AWGN with RFI using single channel FEQ, and AWGN with RFI using multichannel FEQ in accordance with one embodiment of the present invention;

Figure 2 is a system diagram depicting a multichannel FEQ integrated with an ADSL communication system according to one embodiment of the present invention; and

Figure 3 is a flow diagram illustrating a method of estimating multichannel FEQ coefficients for the nth subchannel, $\mathbf{g}(n)$, according to one embodiment of the present invention.

While the above-identified drawing figures exemplify characteristics associated with particular embodiments, other embodiments of the present invention are also contemplated, as noted in the discussion. In all cases, this disclosure presents illustrated embodiments of the present invention by way of representation and not limitation. Numerous other modifications and embodiments can be devised by those skilled in the art which fall within the scope and spirit of the principles of this invention.

Detailed Description of the Preferred Embodiments

The present invention is best understood by considering a system with $n = 1, ..., N$ subchannels which transmits data at time $t = 1, ..., T$. If subchannels are arranged along the rows and times are arranged along the columns, then a N x T transmitted data matrix $\mathbf{X}$ can be written as

$$\mathbf{X} = \begin{bmatrix} X(1,1) & \cdots & X(1,T) \\ \vdots & & \vdots \\ X(N,1) & \cdots & X(N,T) \end{bmatrix} \tag{1}$$

$\mathbf{Y}$, a N x T matrix of received symbols, and $\mathbf{V}$, a N x T noise matrix, are defined in an analogous manner.

In order to implement one embodiment of the present invention, the present inventor designed a N x N equalizer, $\mathbf{G}$, such that

$$\mathbf{G}(n, :) = \underset{\mathbf{G}(n,:)}{\arg\min} E\left[\left|\mathbf{X}(n,t) - \mathbf{G}(n,:)\mathbf{Y}(:,t)\right|^2\right] \tag{2}$$

If the channel matrix $\mathbf{H} = \text{diag}\,(H(1) \ldots H(N))$, and if the received data at time t can be written as

$$\mathbf{Y}(:, t) = \mathbf{H}\mathbf{X}(:, t) + \mathbf{V}(:, t), \tag{3}$$

where the elements of $\mathbf{V}(:, t)$ are uncorrelated, then the zero forcing equalizer $\mathbf{G}$ can be recovered as

$$\mathbf{G} = \text{diag}\left(\frac{1}{H(1)}, \ldots, \frac{1}{H(N)}\right). \tag{4}$$

The minimum mean-square error solution also has a diagonal structure:

$$G = diag\left(\frac{H(1)^*}{|H(1)|^2 + \dfrac{P_x(1)}{P_v(1)}}, \cdots \frac{H(N)^*}{|H(N)|^2 + \dfrac{P_x(N)}{P_v(N)}}\right), \tag{5}$$

where $P_x(k)$ is the power spectral density (PSD) of the input, and $P_v(k)$ is the PSD of the noise on the kth subchannel. These arguments are seen to be the standard one-tap FEQ's such as described by T. Starr, J. Cioffi and P. Silverman, *Understanding Digital Subscriber Line Technology*, Upper Saddle River, NJ: Prentice Hall, 1999, referenced herein before.

The present inventor recognized, however, when there is correlation in the noise matrix **V** (e.g., from a correlated noise source such as RFI), it seems reasonable to consider equalizers **G** that have nonzero elements in addition to the main diagonal. One embodiment can be exemplified by considering the nth subchannel and letting **k**(n) be the indices of the desired nonzero columns of the nth row of **G**. Most preferably, **G**$(n, \mathbf{k}(n))$ can then be found such that

$$X(n, t) = \mathbf{Y}(\mathbf{k}(n), t)^T \mathbf{G}(n, \mathbf{k}(n))^T \tag{6}$$

Letting g$(n) = \mathbf{G}(n, \mathbf{k}(n))^T$, collecting data from time $t = 1, \ldots, T$, and making the obvious substitutions then yields:

$$\begin{bmatrix} X(n,1) \\ \vdots \\ X(n,T) \end{bmatrix} = \begin{bmatrix} \mathbf{Y}(\mathbf{k}(n),1)^T \\ \vdots \\ \mathbf{Y}(\mathbf{k}(n),T)^T \end{bmatrix} \mathbf{g}(n), \tag{7}$$

where

$$\mathbf{x}(n) = \mathbf{Y}(n)\mathbf{g}(n) \tag{8}$$

Therefore, the nth row of the equalizer **G** can be recovered as

$$\mathbf{g}(n) = \mathbf{Y}(n)^{-1}\mathbf{x}(n) \tag{9}$$

This procedure is then repeated for the remaining subchannels to form the complete multichannel FEQ:

$$\mathbf{G} = \begin{bmatrix} \mathbf{g}(1)^T \\ \vdots \\ \mathbf{g}(N)^T \end{bmatrix} \tag{10}$$

The present invention is not so limited however, and it shall be understood that other solutions, including but not limited to, iterative solutions are also possible using least mean-squares (LMS), recursive least-squares (RLS), and their related variants such as discussed by G.-O. Glentis, K. Berberidis and S. Theodoridis, "Efficient least squares adaptive algorithms for FIR transversal filtering," *IEEE Signal Processing Magazine*, vol. 16, no. 4, pp. 13-41, 1999. The nth row, for example, of the multichannel FEQ can be updated as:

$$e(t) = X(n,t) - \mathbf{Y}(\mathbf{k}(n),t)^T \mathbf{g}(n) \tag{11}$$

$$\mathbf{g}(n) = \mathbf{g}(n) + \mu(t)e(t)\mathbf{Y}(\mathbf{k}(n),t)^* \tag{12}$$

for $t = 1, \ldots, T$, where $\mu(t)$ controls the adaptation. Popular choices include:

• Standard LMS:

$$\mu(t) = \alpha, \tag{13}$$

where

$$0 < \alpha < \frac{2}{\lambda_{\max}(\mathbf{R})} \qquad (14)$$

and

$$\mathbf{R} = E\left[\mathbf{Y}(\mathbf{k}(n),t)\mathbf{Y}(\mathbf{k}(n),t)^H\right] \qquad (15)$$

• Normalized LMS (NLMS):

$$\mu(t) = \frac{\alpha}{\beta + \mathbf{Y}(\mathbf{k}(n),t)^H \mathbf{Y}(\mathbf{k}(n),t)}, \qquad (16)$$

where $\alpha \in (0,2)$ and $0 \leq \beta$.

• Power Normalized LMS (PNLMS):

$$\mu(t) = \frac{\alpha}{\sigma^2(t)}, \qquad (17)$$

where $\sigma^2(t) = c\sigma^2(t-1) + |e(t)|^2$, $c \in (0,1)$, and $0 < \alpha < \frac{2}{M}$.

Most preferably, when choosing the nonzero columns of the nth row of $\mathbf{G}$, other than the nth column (which should be selected as this is the column directly correlated with the input through the channel), columns corresponding to subchannels with strong correlations with the nth subchannel should be chosen. These are often neighboring subchannels, or subchannels corresponding to strong RFI sources.

Subchannels with strong RFI can be found via any well-known peak picking algorithm applied to the noise vector $\mathbf{V}(:, t)$. It can be appreciated that when RFI dominates the received signal on a subchannel, then adding a weighed version of the received subchannel with RFI to the desired subchannel n is (almost) equivalent to the

same operation when no data was transmitted on that subchannel. As the RFI and signal power become closer, however, not transmitting data on a subchannel allows that subchannel to be used more effectively with other subchannels in the multichannel FEQ.

A good model for the RFI (or other source of subchannel noise correlation) could potentially be exploited to improve the performance such as discussed by B. Wiese and J. Bingham, "Digital radio frequency cancellation for DMT VDSL," *ANSI T1E1.4/97-460*, Dec. 1997. A positive aspect of the present method however, is that its adaptive nature allows it to be somewhat decoupled from the exact RFI model. Further, the single channel FEQ or an existing RFI model could be used to initialize the present adaptive process.

Table 1 below highlights the channel capacity in Mbps for three different scenarios including AWGN with no RFI using a single channel FEQ, AWGN with RFI using a single channel FEQ, and AWGN with RFI using the present multichannel FEQ. The results were obtained by simulating a downstream ADSL channel with RFI added at the receiver. Three subchannels were used for the design of the multichannel FEQ for the nth subchannel: the nth subchannel, and the two other subchannels with the strongest noise power. The multichannel FEQ coefficients were solved for using the NLMS algorithm. The channel was modeled as 6000 feet of 26 AWG twisted pair copper wire with −140 dBm/Hz additive white Gaussian noise (AWGN) and RFI model 1 impairments such as discussed by ITU Telecommunications Standardization Sector, *G.test.bis.* Study Group 4, Question 15, 2000, referenced herein before. The capacity (*C*) in bits/s (bps) was calculated from:

$$C = f_0 \log_2(1 + SNR),$$

where f_0 is 4000, and SNR is the gap adjusted signal-to-noise ratio after the FEQ.

Table 1: Capacity calculations

Noise	FEQ	Capacity (Mbps)
AWGN	Single channel	10.951
AWGN+RFI	Single channel	5.794
AWGN+RFI	Multichannel	7.681

Figure 1 is a graph illustrating a simulated subchannel SNR for 1) additive white Gaussian noise (AWGN) with no RFI using a single channel FEQ, 2) AWGN with RFI using a single channel FEQ, and 3) AWGN with RFI using the present multichannel FEQ in accordance with one embodiment of the present invention. The results suggest that significant SNR improvements (and corresponding capacity gains) are possible with the present multichannel FEQ.

Figure 2 is a simplified block diagram depicting an ADSL communication system 10 using a multichannel FEQ 12 according to one embodiment of the present invention. At the transmitter, input data 14 to be transmitted is segmented (serial-to-parallel (S/P) converted), as depicted in element 16, into blocks of length N. The nth element is referred to as the nth subchannel. The data is transformed (e.g., in the case of ADSL, by an IFFT as depicted in element 18, and the addition of a cyclic prefix as depicted in element 20) to length $N + P$. The transformed data is next unsegmented, as depicted by element 22 (parallel-to-serial (P/S) converted). The data is then sent through the channel as shown by element 24 (perhaps after additional filtering, mixing, etc. not shown). This channel data is then received by the ADSL receiver, perhaps after filtering, mixing, etc., and generally includes time domain equalization (TEQ) shown by element 26, that is conventionally implemented as an FIR filter. Noise 28, such as RFI discussed herein before, may be introduced into the signal before it is received by the ADSL receiver. The noise that results from RFI at the receiver is deterministically spread by the FFT to neighboring subchannels. As a result, instead of one (or a few) subchannels being effected by the narrowband impairment, many subchannels are effected. The resulting loss of signal-to-noise ratio (SNR) can unacceptably limit the capacity of the communication channel 24. With continued reference now to Figure 2, the data is S/P

converted as shown by element 30, into blocks of length $N + P$, subsequent to time domain equalization 26. The data is then transformed (e.g., in the case of ADSL, by removing the cyclic prefix as shown by element 32 and a FFT as shown by element 34) to length N. Following this transformation process, the present multichannel FEQ 12 is applied to each block of data. The multichannel FEQ 12 output data for the nth subchannel can then be expressed as

$$x(n,t) = \mathbf{Y}(\mathbf{k}(n),t)^{T} \mathbf{g}(n) .$$

as discussed herein before with reference to equation (7). The output data from the multichannel FEQ 12 is the P/S converted, as shown by element 36, to form an estimate of the original data.

Figure 3 is a flow diagram illustrating a method 100 of estimating multichannel FEQ coefficients for the nth subchannel, $\mathbf{g}(n)$, according to one embodiment of the present invention. As discussed above, the present method relates to T blocks of transmitted data, $\mathbf{X}(:, t)$, $t = 1, ..., T$, and T blocks of received data, $\mathbf{Y}(:, t)$, $t = 1, ..., T$ depicted by elements 102 and 104 respectively. The received data can then be used to determine a set of subchannels, $\mathbf{k}(n)$, for the multichannel FEQ 12 to use in conjunction with subchannel n, for each subchannel n used to transmit data, as shown by element 106. The set of subchannels, $\mathbf{k}(n)$, includes the nth subchannel and one or more of the following: the nth subchannel's neighboring subchannels; subchannels where RFI is located; and subchannels where the noise power is (relatively) strong. Finally, the multichannel FEQ coefficients for the nth subchannel, $\mathbf{g}(n)$, are generated as shown by element 108, via equation (2) using all of the received data at once, according to equation (9), or adaptively, using a block of data at a time, according to equations (11) and (12). These multichannel FEQ coefficients are then used in a complex multiply operation to adjust for the gain and phase of the effective channel response in each subsymbol.

In view of the above, it can be seen the present invention presents a significant advancement in the art of communication between subscribers over shared media. Further, this invention has been described in considerable detail in order to provide those skilled in the data communication art with the information needed to apply the novel

principles and to construct and use such specialized components as are required. In view of the foregoing descriptions, it should be apparent that the present invention represents a significant departure from the prior art in construction and operation. However, while particular embodiments of the present invention have been described herein in detail, it is to be understood that various alterations, modifications and substitutions can be made therein without departing in any way from the spirit and scope of the present invention, as defined in the claims which follow.

WHAT IS CLAIMED IS:

1.   A method of canceling communication system noise interference, the method comprising the steps of:

     a) receiving T blocks of data, $\mathbf{Y}(:, t)$, $t = 1, \ldots, T$, comprising T blocks of data, $\mathbf{X}(:,t)$, $t = 1, \ldots, T$, transmitted over predetermined subchannels;

     b) determining a set of subchannels, $\mathbf{k}(n)$, for the multichannel frequency domain equalizer (FEQ) for subchannel n;

     c) generating multichannel FEQ coefficients, $\mathbf{g}(n)$, for the nth subchannel used to transmit the data; and

     d) performing multichannel (FEQ) for subchannel n using the generated multichannel FEQ coefficients.

2.   The method of canceling communication system noise interference according to claim 1 wherein steps b-d are repeated for each subchannel n used to transmit the T blocks of data.

3.   The method of canceling communication system noise interference according to claim 1 wherein the step of determining a set of subchannels, $\mathbf{k}(n)$, for a subchannel n used to transmit the T blocks of data includes selecting subchannel n.

4.   The method of canceling communication system noise interference according to claim 3 wherein the step of determining a set of subchannels, $\mathbf{k}(n)$, for a subchannel n used to transmit the T blocks of data further includes selecting neighboring subchannels to subchannel n.

5.   The method of canceling communication system noise interference according to claim 3 wherein the step of determining a set of subchannels, $\mathbf{k}(n)$, for a subchannel n used to transmit the T blocks of data further includes selecting subchannels where radio frequency interference is located.

6.   The method of canceling communication system noise interference according to claim 3 wherein the step of determining a set of subchannels, $\mathbf{k}(n)$, for a subchannel n used to transmit the T blocks of data further includes selecting subchannels having predetermined noise characteristics.

7.   The method of canceling communication system noise interference according to claim 1 wherein the step of generating multichannel FEQ coefficients, $\mathbf{g}(n)$, for subchannel n, comprises solving the equation $\mathbf{g}(n) = \mathbf{Y}(n)^{-1}\mathbf{x}(n)$, where $\mathbf{Y}(n)^{-1}$ is the pseudoinverse of a matrix of received data for subchannels $\mathbf{k}(n)$, and $\mathbf{x}(n)$ is a vector of transmitted data for subchannel n.

8.   The method of canceling communication system noise interference according to claim 7 wherein $\mathbf{g}(n)$ is determined adaptively using a block of received data at a time according to an equation defined by: $\mathbf{g}(n) = \mathbf{g}(n) + \mu(t)e(t)\mathbf{Y}(\mathbf{k}(n),t)^{*}$, where $\mathbf{g}(n)$ is the vector of multichannel FEQ coefficients for subchannel n and $\mathbf{Y}(\mathbf{k}(n), t)^{*}$ is the conjugate of a matrix of received data for subchannels $\mathbf{k}(n)$.

9.   The method of canceling communication system noise interference according to claim 8 wherein values of $e(t)$ are determined according to an equation defined by: $e(t) = X(n,t) - \mathbf{Y}(\mathbf{k}(n),t)^{T}\mathbf{g}(n)$, where $X(n, t)$ is the transmitted data for subchannel n at time t, and $\mathbf{Y}(\mathbf{k}(n),t)^{T}$ is the transpose of a matrix of received data for subchannels $\mathbf{k}(n)$.

10.   The method of canceling communication system noise interference according to claim 8 wherein $\mu(t)$ controls the adaptation according to least mean squares and has a value determined according to an equation defined by: $\mathbf{R} = E\left[\mathbf{Y}(\mathbf{k}(n),t)\mathbf{Y}(\mathbf{k}(n),t)^{H}\right]$, where $\mathbf{Y}(\mathbf{k}(n),t)^{H}$ is the conjugate transpose of a matrix of received data for subchannels $\mathbf{k}(n)$.

11. The method of canceling noise interference according to claim 8 wherein $\mu(t)$ controls the adaptation according to normalized least mean squares and has a value determined according to an equation defined by: $\mu(t) = \dfrac{\alpha}{\beta + \mathbf{Y}(\mathbf{k}(n),t)^H \mathbf{Y}(\mathbf{k}(n),t)}$,

where $\alpha \in (0,2)$, $0 \le \beta$, and $\mathbf{Y}(\mathbf{k}(n),t)$ is a matrix of received data for subchannels $\mathbf{k}(n)$.

12. The method of canceling noise interference according to claim 8 wherein $\mu(t)$ controls the adaptation according to power normalized least mean squares and has a value α determined according to an equation defined by: $\mu(t) = \dfrac{\alpha}{\sigma^2(t)}$,

where $\sigma^2(t) = c\sigma^2(t-1) + |e(t)|^2$, $c \in (0,1)$, and $0 < \alpha < \dfrac{2}{M}$.

13. A system for canceling communication system noise interference, the system comprising:

a multichannel frequency domain equalizer configured to receive T blocks of data, $\mathbf{Y}(:, t)$, $t = 1, \ldots, T$, comprising T blocks of data, $\mathbf{X}(:,t)$, $t = 1, \ldots, T$, transmitted over predetermined subchannels, wherein the multichannel frequency domain equalizer is operational to generate multichannel frequency domain equalization (FEQ) coefficients, $\mathbf{g}(n)$, associated with the nth subchannel used to transmit the data, and to perform multichannel FEQ for the nth subchannel using the generated multichannel FEQ coefficients, and further wherein the FEQ coefficients are associated with a set of subchannels, $\mathbf{k}(n)$, for the nth subchannel used to transmit the T blocks of data.

14. The system according to claim 13 wherein the FEQ is operational to increase a subchannel signal-to-noise ratio beyond that achievable using a single channel FEQ.

15. The system according to claim 13 wherein the FEQ is operational to cancel correlated subchannel noise caused by deterministic noise spreading associated with a plurality of subchannels.

16.   The system according to claim 13 wherein the FEQ is operational to increase achievable digital subscriber network data rate beyond that achievable using a single channel FEQ.

Abstract of the Disclosure

A multichannel frequency domain equalizer improves the subchannel signal to noise ratio by canceling correlated noise that is caused by deterministic spreading at the receiver that introduces correlation into the subchannel noise vector.
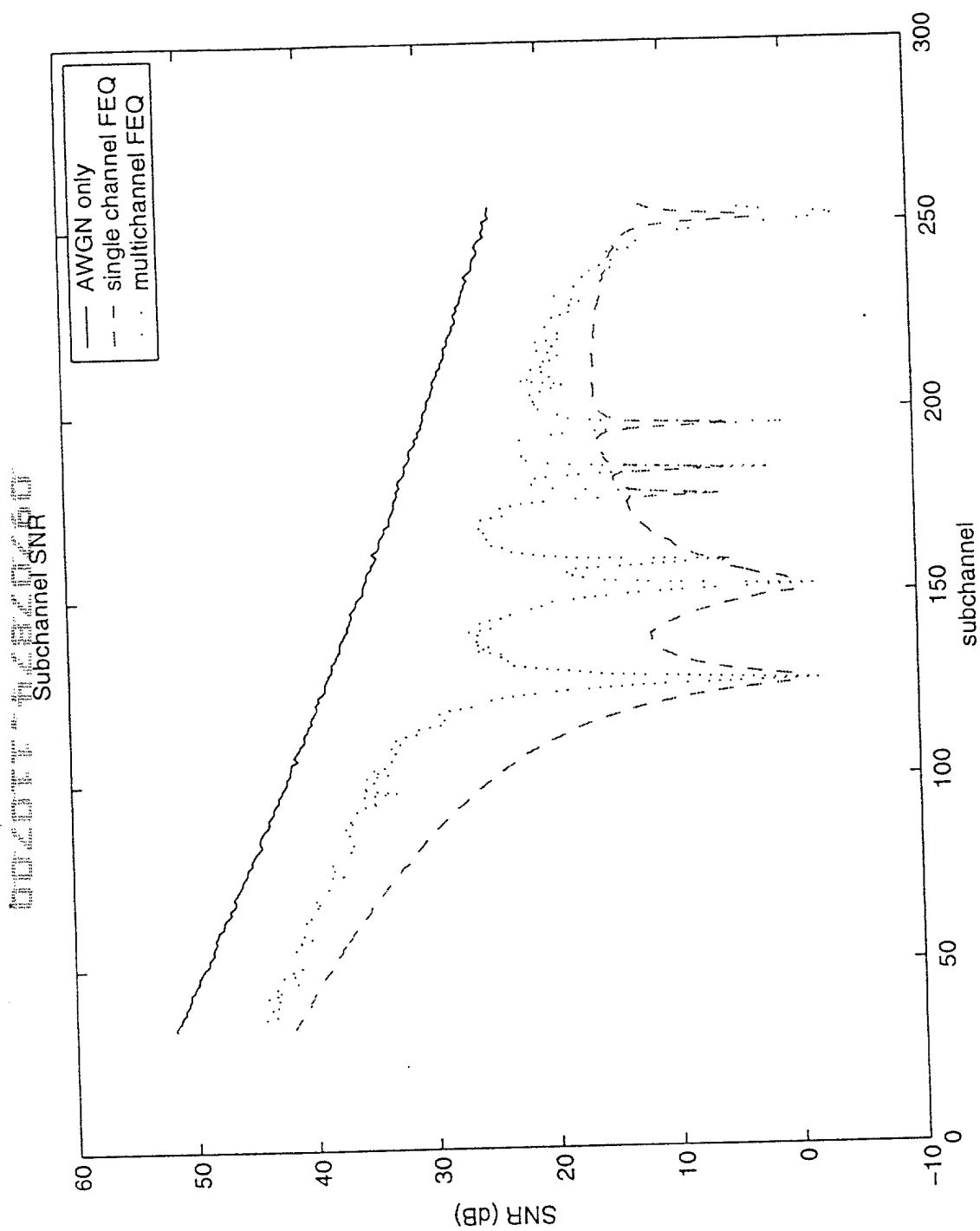
Figure 1

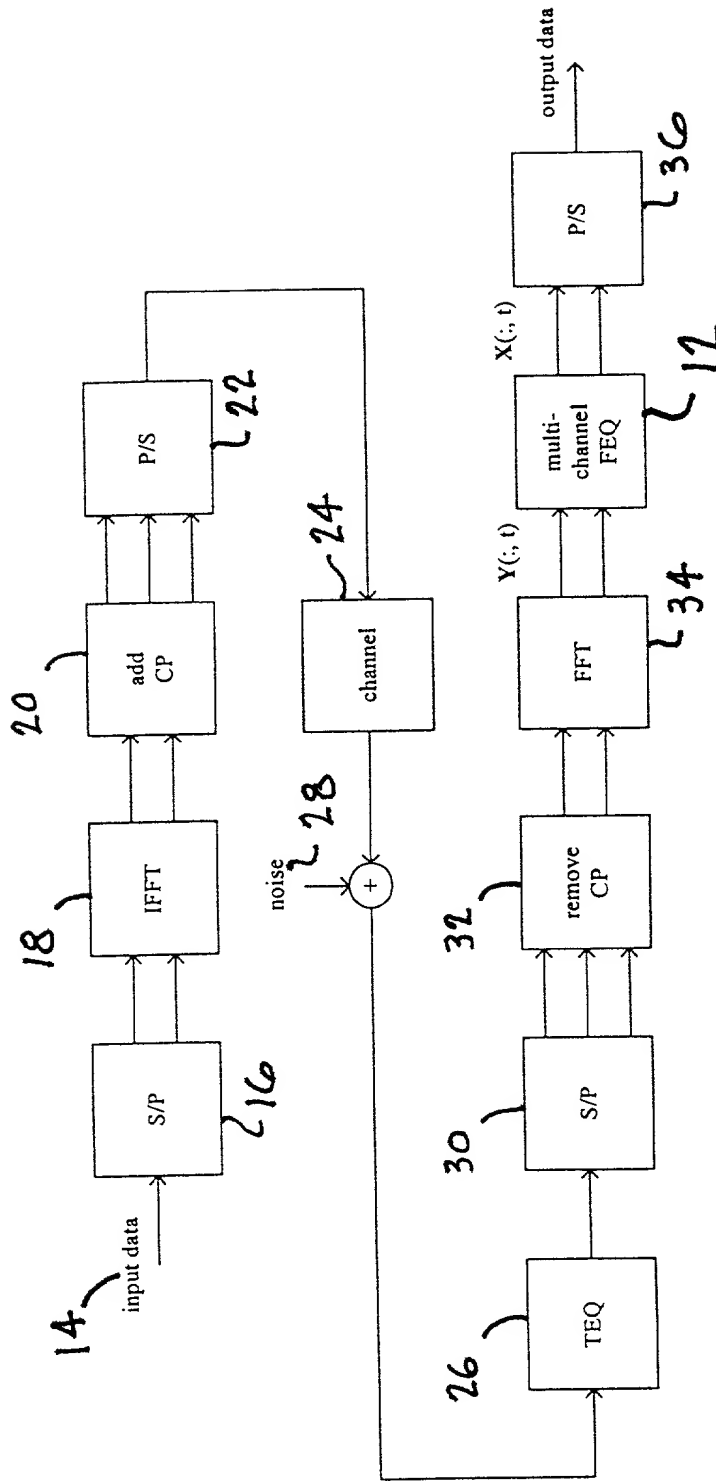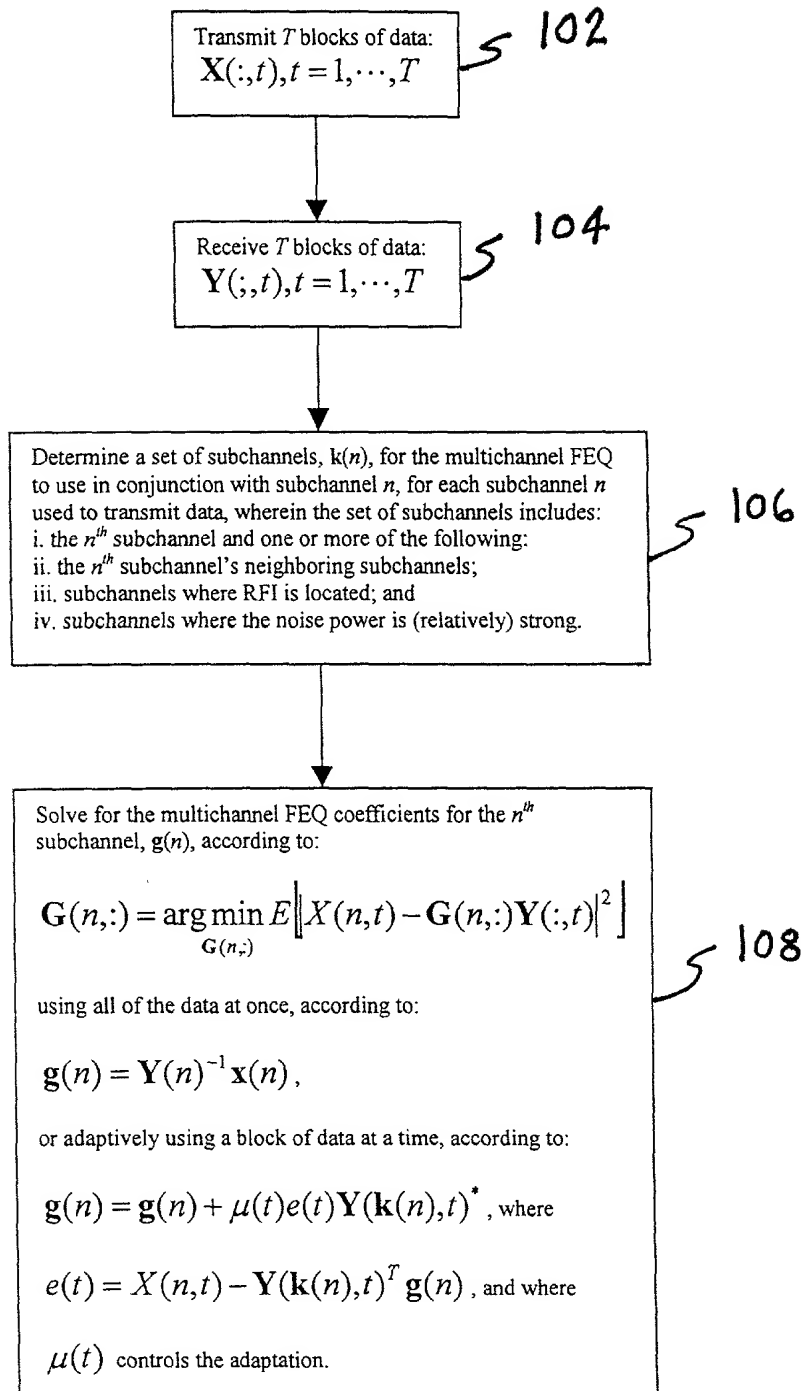Figure 2

```
                    ┌─────────────────────────────┐
                    │ Transmit T blocks of data:  │      ╭ 102
                    │ X(:,t), t = 1,···,T          │─╮  5
                    └─────────────────────────────┘
```

$$\text{Transmit } T \text{ blocks of data:}$$
$$\mathbf{X}(:,t), t = 1,\cdots,T$$

Receive T blocks of data:
$$\mathbf{Y}(;,t), t = 1,\cdots,T$$

Determine a set of subchannels, k(n), for the multichannel FEQ
to use in conjunction with subchannel n, for each subchannel n
used to transmit data, wherein the set of subchannels includes:
i. the nth subchannel and one or more of the following:
ii. the nth subchannel's neighboring subchannels;
iii. subchannels where RFI is located; and
iv. subchannels where the noise power is (relatively) strong.

Solve for the multichannel FEQ coefficients for the nth
subchannel, g(n), according to:

$$\mathbf{G}(n,:) = \arg\min_{\mathbf{G}(n,:)} E\left[\left\|X(n,t) - \mathbf{G}(n,:)\mathbf{Y}(:,t)\right\|^2\right]$$

using all of the data at once, according to:

$$\mathbf{g}(n) = \mathbf{Y}(n)^{-1}\mathbf{x}(n),$$

or adaptively using a block of data at a time, according to:

$$\mathbf{g}(n) = \mathbf{g}(n) + \mu(t)e(t)\mathbf{Y}(\mathbf{k}(n),t)^*, \text{ where}$$

$$e(t) = X(n,t) - \mathbf{Y}(\mathbf{k}(n),t)^T \mathbf{g}(n), \text{ and where}$$

$\mu(t)$ controls the adaptation.

Figure 3

APPLICATION FOR UNITED STATES PATENT
DECLARATION AND POWER OF ATTORNEY

As a below named inventor, I declare that my residence, post office address and citizenship are as stated below next to my name; that I verily believe that I am the original, first and sole inventor if only one name is listed below, or an original, first and joint inventor if plural inventors are named below, of the subject matter which is claimed and for which a patent is sought on the invention entitled as set forth below, which is described in the attached specification; that I have reviewed and understand the contents of the specification, including the claims, as amended by any amendment specifically referred to in the oath or declaration; that no application for patent or inventor's certificate on this invention has been filed by me or my legal representatives or assigns in any country foreign to the United States of America; and that I acknowledge my duty to disclose information which is material to the patentability of this application in accordance with Title 37, Code of Federal Regulations, section 1.56;

I further declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true, and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under section 1001 of Title 18 of the United States Code, and that such willful false statements may jeopardize the validity of the application or any patent issuing thereon.

TITLE OF INVENTION:

MULTI-CHANNEL FREQUENCY DOMAIN EQUALIZER FOR RADIO FREQUENCY INTERFERENCE CANCELLATION

POWER OF ATTORNEY: I HEREBY APPOINT THE FOLLOWING ATTORNEYS TO PROSECUTE THIS APPLICATION AND TRANSACT ALL BUSINESS IN THE PATENT AND TRADEMARK OFFICE CONNECTED THEREWITH

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SIGNATURE OF INVENTOR:	SIGNATURE OF INVENTOR:	SIGNATURE OF INVENTOR:
DATE: *Nov 3, 2000*	DATE:	DATE: